

# MECH 577 Optimum Design

## Fall 2010

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Suite 855 of West Tower, Room 813

Office Hours: Tue & Wed 3:00–4:00

**On-line Tutoring:** Send your queries to [angeles@cim.mcgill.ca](mailto:angeles@cim.mcgill.ca). Computation code and updates on the course are available at

<http://www.cim.mcgill.ca/~rmsl/Index/index.htm>

### Course Outline

**Objective:** To lay the foundations for the development of a methodology that allows the formulation and the solution of engineering design tasks as optimization problems.

### Topics

1. The role of optimization within the design process. Design methodology and design philosophy. Design variables and design space.
2. Single-variable optimization: Unimodality assumption. Solution methods: Dichotomous search; Fibonacci search; and golden-section search.
3. Background on multivariable optimization. The numerical solution of *determined* systems of linear and nonlinear equations: LU-decomposition, a.k.a. Gaussian elimination; the Cholesky decomposition of positive-semidefinite matrices; the Newton-Raphson method. The numerical solution of *overdetermined* systems of linear and nonlinear equations: orthogonalization methods for linear systems; the Newton-Gauss method for nonlinear systems. Numerical conditioning.

### First Class Test

4. Unconstrained multivariable optimization. First- and second-order normality conditions. Direct methods: Hooke and Jeeves; Powell's conjugate directions; Nelder-Mead's simplex method. Gradient methods: Cauchy's steepest descent; Fletcher-Reeves' conjugate gradient; and quasi-Newton methods. Newton methods: the Newton-Raphson and the Levenberg-Marquardt methods.
5. Equality-constrained optimization: The first- and second-order normality conditions. Primal and dual forms. Linear quadratic problems: minimum-norm problems under linear constraints; least-square problems subject to linear constraints. Linear least-square problems under quadratic constraints.

### Second Class Test—Only Material Not Covered in CT1

6. The orthogonal-decomposition algorithm (ODA). Application to equality constrained linear and nonlinear least-square problems. Application to arbitrary objective functions: Hessian-stabilization methods.
7. Inequality-constrained problems: The Karush-Kuhn-Tucker conditions. Direct and indirect methods. Indirect methods: penalty functions and slack variables.
8. Advanced topics: multiobjective optimization and stochastic methods.

### **Third Class Test—Only Material Not Covered in CT1 & CT2**

**Marking Scheme:** The final mark is computed as the average of three projects (total of 67%) and three open-book quizzes (33%), the third one scheduled for the final day of lectures, Friday December 3rd. Individual project marks are based on (a) technical content (2/3 of total mark) and (b) presentation (1/3 of total mark).

**Guidelines for Project Reports:** Read `rppt-gd1ns0100827.pdf`, which is posted on the course website, and handed out together with the Course Outline.

#### **Bibliography:**

Angeles, J., 2010, *MECH 577 Optimum Design Lecture Notes*, Department of Mechanical Engineering, McGill University, Montreal.

Boyd, S. and Vandenberghe, L., 2004, *Convex Optimization*, Cambridge University Press, Cambridge.

Luenberger, D., 1984, *Linear and Nonlinear Programming*, Second Edition, Addison-Wesley Publishing Company, Reading, MA.

Rao, S.S., 1996, *Engineering Optimization*, John Wiley & Sons, Inc., New York.

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