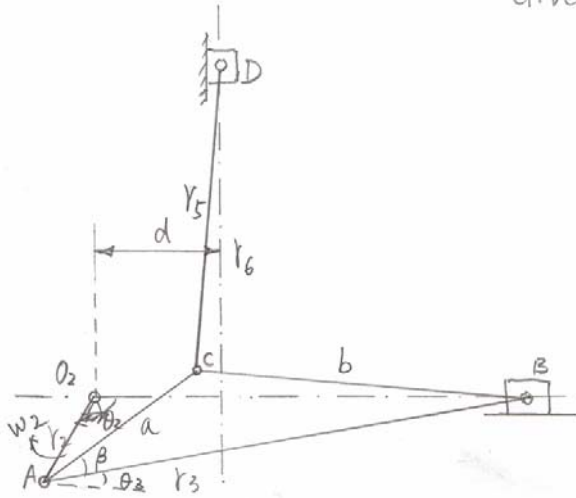


Assignment #5.

Problem 1.



Given: $w_2 = 42 \text{ rad/s cw}$, $\dot{\theta}_2 = 0$, $\theta_2 = -120^\circ$.

$R_{AO_2} = r_2 = 2 \text{ in}$, $R_{BA} = r_3 = 10 \text{ in}$.

$R_{CA} = a = 4 \text{ in}$, $R_{CB} = b = 7 \text{ in}$

$R_{BO_2} = r_1$, $d = 3 \text{ in}$.

$R_{DC} = r_5 = 8 \text{ in}$.

Note: $\theta_3 = 10^\circ$, $\beta = 34^\circ$, $\theta_5 = 83^\circ$.

The Velocity results are obtained by previous assignment solution.

$\dot{\theta}_3 = -4.26 \text{ rad/s}$, $\dot{r}_1 = -65.3 \text{ m/s}$

$\dot{\theta}_5 = 7.67 \text{ rad/s}$, $v_D = 22.25 \text{ m/s}$.

First Loop closure:

$$\vec{R}_{AO_2} + \vec{R}_{BA} - \vec{R}_{BO_2} = \vec{0}$$

↓

$$\left. \begin{aligned} r_2 \cos \theta_2 + r_3 \cos \theta_3 - r_1 \cos \theta_1 &= 0 \\ r_2 \sin \theta_2 + r_3 \sin \theta_3 - r_1 \sin \theta_1 &= 0 \end{aligned} \right\}$$

↓ Differentiate with time, $\dot{\theta}_1 = 0$ also.

$$\left. \begin{aligned} -r_2 \sin \theta_2 \cdot \dot{\theta}_2 - r_3 \sin \theta_3 \cdot \dot{\theta}_3 - \dot{r}_1 &= 0 \\ r_2 \cos \theta_2 \cdot \dot{\theta}_2 + r_3 \cos \theta_3 \cdot \dot{\theta}_3 &= 0 \end{aligned} \right\}$$

↓ $\frac{d}{dt}$

$$\left. \begin{aligned} -r_2 \cos \theta_2 \cdot \dot{\theta}_2^2 - r_2 \sin \theta_2 \cdot \ddot{\theta}_2 - r_3 \cos \theta_3 \cdot \dot{\theta}_3^2 - r_3 \sin \theta_3 \cdot \ddot{\theta}_3 - \ddot{r}_1 &= 0 \\ -r_2 \sin \theta_2 \cdot \dot{\theta}_2^2 + r_2 \cos \theta_2 \cdot \ddot{\theta}_2 - r_3 \sin \theta_3 \cdot \dot{\theta}_3^2 + r_3 \cos \theta_3 \cdot \ddot{\theta}_3 &= 0 \end{aligned} \right\}$$

↓ in matrix form.

$$\begin{bmatrix} -1 & -r_3 \sin \theta_3 \\ 0 & r_3 \cos \theta_3 \end{bmatrix} \begin{bmatrix} \ddot{r}_1 \\ \ddot{\theta}_3 \end{bmatrix} = \begin{bmatrix} r_2 \cos \theta_2 \cdot \dot{\theta}_2^2 + r_2 \sin \theta_2 \cdot \ddot{\theta}_2 + r_3 \cos \theta_3 \cdot \dot{\theta}_3^2 \\ r_2 \sin \theta_2 \cdot \dot{\theta}_2^2 - r_2 \cos \theta_2 \cdot \ddot{\theta}_2 + r_3 \sin \theta_3 \cdot \dot{\theta}_3^2 \end{bmatrix}$$

Invert coefficient matrix.

(2)

$$\rightarrow \begin{bmatrix} \ddot{r}_1 \\ \ddot{\theta}_3 \end{bmatrix} = \begin{bmatrix} -1 & \frac{\sin\theta_2}{\cos\theta_3} \\ 0 & \frac{1}{r_3 \cos\theta_3} \end{bmatrix} \begin{bmatrix} r_2 \cos\theta_2 \ddot{\theta}_2^2 + r_2 \sin\theta_2 \ddot{\theta}_2 + r_3 \cos\theta_3 \ddot{\theta}_3^2 \\ r_2 \sin\theta_2 \ddot{\theta}_2^2 - r_2 \cos\theta_2 \ddot{\theta}_2 + r_3 \sin\theta_3 \ddot{\theta}_3^2 \end{bmatrix}$$

$$\ddot{\theta}_2 = 0 \rightarrow \left. \begin{array}{l} \ddot{r}_1 = 2118 \text{ in/s}^2 \\ \ddot{\theta}_3 = -307 \text{ rad/s}^2 \end{array} \right\} \rightarrow \left\{ \begin{array}{l} A_B = 2118 \text{ in/s}^2 \rightarrow \\ \alpha_3 = -307 \text{ rad/s}^2 \text{ cw} \end{array} \right.$$

Second Loop closure:

$$\vec{R}_{AO_2} + \vec{R}_{CA} + \vec{R}_{D_6C} - \vec{R}_{D_6O_2} = \vec{0}$$

$$\downarrow \left. \begin{array}{l} \vec{R}_{D_6O_2}^x + \vec{R}_{D_6O_2}^y \end{array} \right\} \rightarrow \left\{ \begin{array}{l} r_6 = R_{D_6O_2}^y \\ d = R_{D_6O_2}^x \end{array} \right.$$

$$r_2 \cos\theta_2 + a \cos(\theta_3 + \beta) + r_5 \cos\theta_5 - d = 0$$

$$r_2 \sin\theta_2 + a \sin(\theta_3 + \beta) + r_5 \sin\theta_5 - r_6 = 0$$

$\downarrow \frac{d}{dt}$, Note: β is a constant.

$$-r_2 \sin\theta_2 \cdot \dot{\theta}_2 - a \sin(\theta_3 + \beta) \cdot \dot{\theta}_3 - r_5 \sin\theta_5 \cdot \dot{\theta}_5 = 0$$

$$r_2 \cos\theta_2 \cdot \dot{\theta}_2 + a \cos(\theta_3 + \beta) \cdot \dot{\theta}_3 + r_5 \cos\theta_5 \cdot \dot{\theta}_5 - \dot{r}_6 = 0$$

$\downarrow \frac{d}{dt}$

$$-r_2 \cos\theta_2 \dot{\theta}_2^2 - r_2 \sin\theta_2 \ddot{\theta}_2 - a \cos(\theta_3 + \beta) \dot{\theta}_3^2 - a \sin(\theta_3 + \beta) \ddot{\theta}_3 - r_5 \cos\theta_5 \dot{\theta}_5^2 - r_5 \sin\theta_5 \ddot{\theta}_5 = 0$$

$$-r_2 \sin\theta_2 \dot{\theta}_2^2 + r_2 \cos\theta_2 \ddot{\theta}_2 - a \sin(\theta_3 + \beta) \dot{\theta}_3^2 + a \cos(\theta_3 + \beta) \ddot{\theta}_3 - r_5 \sin\theta_5 \dot{\theta}_5^2 + r_5 \cos\theta_5 \ddot{\theta}_5 - \ddot{r}_6 = 0$$

\downarrow in matrix form.

$$\begin{bmatrix} r_5 \sin\theta_5 & 0 \\ r_5 \cos\theta_5 & -1 \end{bmatrix} \begin{bmatrix} \ddot{\theta}_5 \\ \ddot{r}_6 \end{bmatrix} = \begin{bmatrix} -r_2 \cos\theta_2 \dot{\theta}_2^2 - r_2 \sin\theta_2 \ddot{\theta}_2 - a \cos(\theta_3 + \beta) \dot{\theta}_3^2 - a \sin(\theta_3 + \beta) \ddot{\theta}_3 - r_5 \cos\theta_5 \dot{\theta}_5^2 \\ -r_2 \sin\theta_2 \dot{\theta}_2^2 + r_2 \cos\theta_2 \ddot{\theta}_2 + a \sin(\theta_3 + \beta) \dot{\theta}_3^2 + a \cos(\theta_3 + \beta) \ddot{\theta}_3 + r_5 \sin\theta_5 \dot{\theta}_5^2 - r_5 \cos\theta_5 \ddot{\theta}_5 \end{bmatrix}$$

(3)

invert coefficient matrix.

$$\ddot{\theta}_2 = 0 \rightarrow \begin{bmatrix} \ddot{\theta}_5 \\ \ddot{r}_6 \end{bmatrix} = \begin{bmatrix} \frac{1}{r_5 \sin \theta_5} & 0 \\ \frac{\cos \theta_5}{r_5 \sin \theta_5} & -1 \end{bmatrix} \begin{bmatrix} -r_2 \cos \theta_2 \cdot \dot{\theta}_2^2 - a \cos(\theta_3 + \beta) \dot{\theta}_3^2 - a \sin(\theta_3 + \beta) \ddot{\theta}_3 - r_5 \cos \theta_5 \cdot \dot{\theta}_5^2 \\ r_2 \sin \theta_2 \cdot \dot{\theta}_2^2 + a \sin(\theta_3 + \beta) \dot{\theta}_3^2 - a \cos(\theta_3 + \beta) \ddot{\theta}_3 + r_5 \sin \theta_5 \cdot \dot{\theta}_5^2 \end{bmatrix}$$

$$\therefore \left. \begin{array}{l} \ddot{\theta}_5 = 315.8 \text{ rad/s}^2 \\ \ddot{r}_6 = 1962 \text{ in/s}^2 \end{array} \right\} \rightarrow \left\{ \begin{array}{l} \omega_5 = 315.8 \text{ rad/s}^2 \text{ ccw} \\ A_D = 19.62 \text{ in/s}^2 \uparrow \end{array} \right.$$

Vector equation for point c: $\vec{R}_{AO_2} + \vec{R}_{CA} - \vec{R}_{CO_2} = \vec{0}$

$$\downarrow$$

$$\left. \begin{array}{l} r_2 \cos \theta_2 + a \cos(\theta_3 + \beta) - x_c = 0 \\ r_2 \sin \theta_2 + a \sin(\theta_3 + \beta) - y_c = 0 \end{array} \right\}$$

$$\downarrow d/dt$$

$$\left. \begin{array}{l} -r_2 \sin \theta_2 \cdot \dot{\theta}_2 - a \sin(\theta_3 + \beta) \dot{\theta}_3 - \dot{x}_c = 0 \\ r_2 \cos \theta_2 \cdot \dot{\theta}_2 + a \cos(\theta_3 + \beta) \dot{\theta}_3 - \dot{y}_c = 0 \end{array} \right\}$$

 $\downarrow d/dt$

$$\left. \begin{array}{l} -r_2 \cos \theta_2 \cdot \dot{\theta}_2^2 - r_2 \sin \theta_2 \cdot \ddot{\theta}_2 - a \cos(\theta_3 + \beta) \dot{\theta}_3^2 - a \sin(\theta_3 + \beta) \ddot{\theta}_3 - \ddot{x}_c = 0 \\ -r_2 \sin \theta_2 \cdot \dot{\theta}_2^2 + r_2 \cos \theta_2 \cdot \ddot{\theta}_2 - a \sin(\theta_3 + \beta) \dot{\theta}_3^2 + a \cos(\theta_3 + \beta) \ddot{\theta}_3 - \ddot{y}_c = 0 \end{array} \right\}$$

 \downarrow

$$\left. \begin{array}{l} \ddot{x}_c = 2565 \text{ in/s}^2 \\ \ddot{y}_c = 2121 \text{ in/s}^2 \end{array} \right\} \rightarrow A_c = 3328 \text{ in/s}^2 \nearrow$$

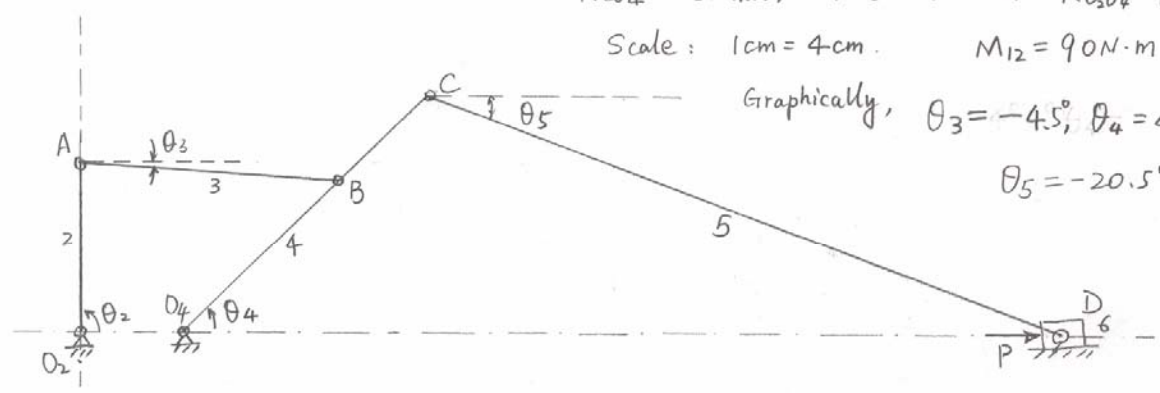
Problem 2. (Figure 14.6. Page 465 in book J. J. Uicker, et. al.)

Given: $R_{A0_2} = 100 \text{ mm}$, $R_{BA} = 150 \text{ mm}$, $R_{B0_4} = 125 \text{ mm}$,
 $R_{C0_4} = 200 \text{ mm}$, $R_{CD} = 400 \text{ mm}$, $R_{O_2O_4} = 60 \text{ mm}$.

Scale: $1 \text{ cm} = 4 \text{ cm}$. $M_{12} = 90 \text{ N}\cdot\text{m}$ ccw.

Graphically, $\theta_3 = -4.5^\circ$, $\theta_4 = 45^\circ$

$\theta_5 = -20.5^\circ$.



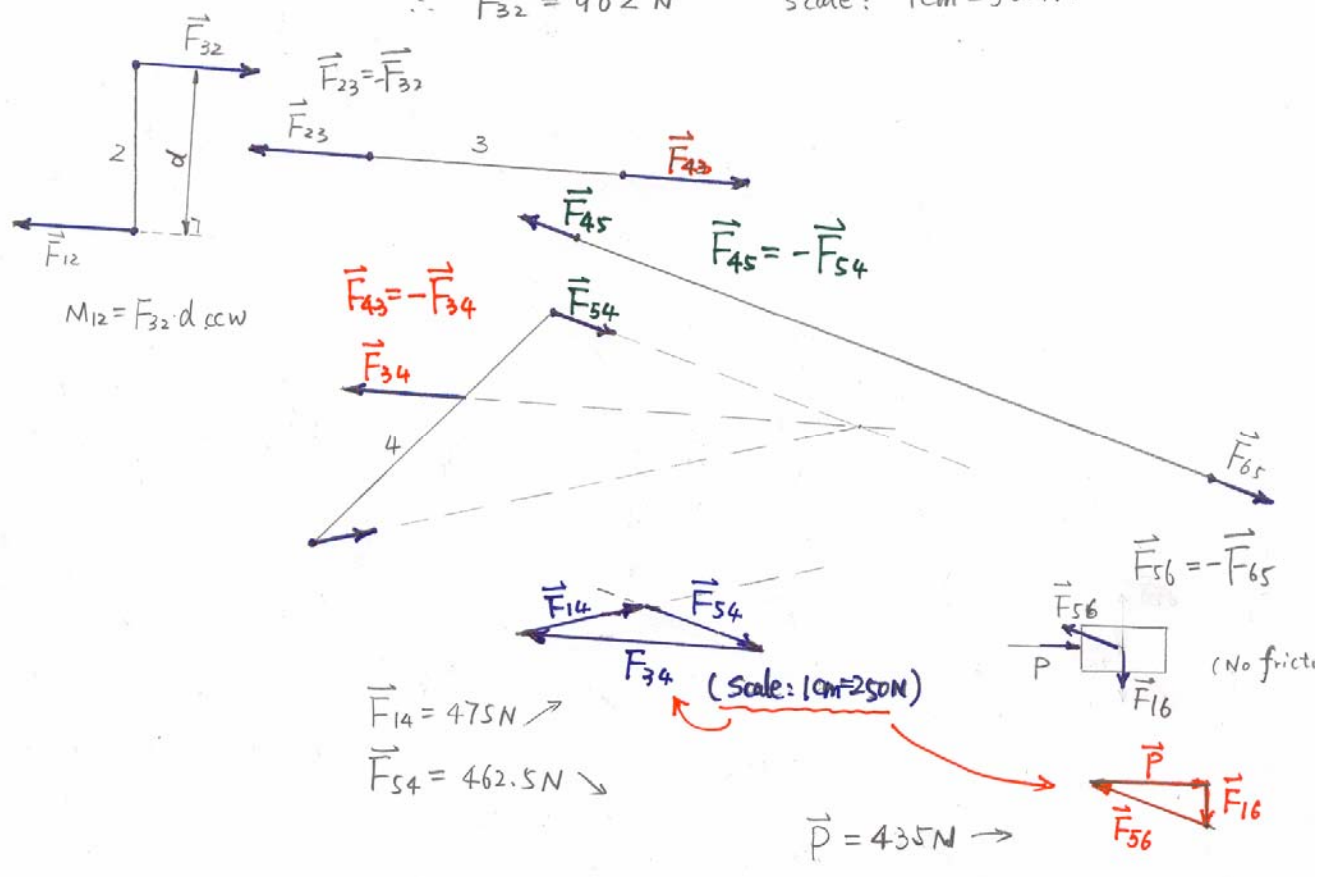
Kinematic Analysis: $\vec{R}_{A0_2} = R_{A0_2}(\cos\theta_2\hat{i} + \sin\theta_2\hat{j}) = 100\hat{j}$.

$\vec{R}_{BA} = R_{BA}(\cos\theta_3\hat{i} + \sin\theta_3\hat{j}) = 149.6\hat{i} - 10.5\hat{j}$, $\vec{R}_{C0_4} = 141.4\hat{i} + 141.4\hat{j}$

$\vec{R}_{Dc} = 374.7\hat{i} - 141.2\hat{j}$, $\vec{R}_{B0_4} = 88.3\hat{i} + 88.3\hat{j}$

Force Analysis: $M_{12} = 90 \text{ N}\cdot\text{m}$, $\vec{M}_{12} = -\vec{R}_{A0_2} \times \vec{F}_{32}$.

$\therefore F_{32} = 902 \text{ N}$ Scale: $1 \text{ cm} = 500 \text{ N}$.



(5)

Analytically, starting with body 2,

$$\vec{F}_{12} = -\vec{F}_{32}$$

$$\sum \vec{M}_{O_2} = \vec{M}_{12} + \vec{R}_{AO_2} \times \vec{F}_{32} = \vec{0} \rightarrow \vec{M}_{12} = -\vec{R}_{AO_2} \times \vec{F}_{32}$$

$$90 \hat{k} \text{ (N}\cdot\text{m)} = 90000 \hat{k} \text{ (N}\cdot\text{mm)} = \vec{M}_{12} = -100 \hat{j} \times (F_{32} \cos \theta_3 \hat{i} - F_{32} \sin \theta_3 \hat{j})$$

$$= -100 F_{32} \cos \theta_3 \hat{k}$$

$$\therefore F_{32} = 902 \text{ N} \quad \vec{F}_{32} = 899 \hat{i} - 70.8 \hat{j} \text{ (N)}$$

$$\vec{F}_{23} = -\vec{F}_{32} = -899 \hat{i} + 70.8 \hat{j} \text{ (N)}$$

$$\rightarrow \text{Link 3: } \vec{F}_{23} + \vec{F}_{43} = \vec{0} \rightarrow \vec{F}_{43} = -\vec{F}_{23} = 899 \hat{i} - 70.8 \hat{j} \text{ (N)}$$

$$\vec{F}_{34} = -\vec{F}_{43} = -899 \hat{i} + 70.8 \hat{j} \text{ (N)}$$

→ Free body diagram of link 4:

$$\vec{0} = \vec{M}_{O_4} = \vec{R}_{BO_4} \times \vec{F}_{34} + \vec{R}_{CO_4} \times \vec{F}_{54} = \vec{0}$$

$$= (88.3 \hat{i} + 88.3 \hat{j}) \times (-899 \hat{i} + 70.8 \hat{j}) + (141.4 \hat{i} + 141.4 \hat{j}) \times (F_{54} \cos \theta_5 \hat{i} + F_{54} \sin \theta_5 \hat{j})$$

$$= 85633 \hat{k} + F_{54} (-182 \hat{k})$$

$$F_{54} = 470.5 \text{ N} \quad \rightarrow \vec{F}_{54} = 440.7 \hat{i} - 164.8 \hat{j} \text{ (N)}$$

$$\vec{F}_{14} + \vec{F}_{54} + \vec{F}_{34} = \vec{0} \rightarrow \vec{F}_{14} = -\vec{F}_{54} - \vec{F}_{34} = 458.3 \hat{i} + 94 \hat{j} \text{ (N)}$$

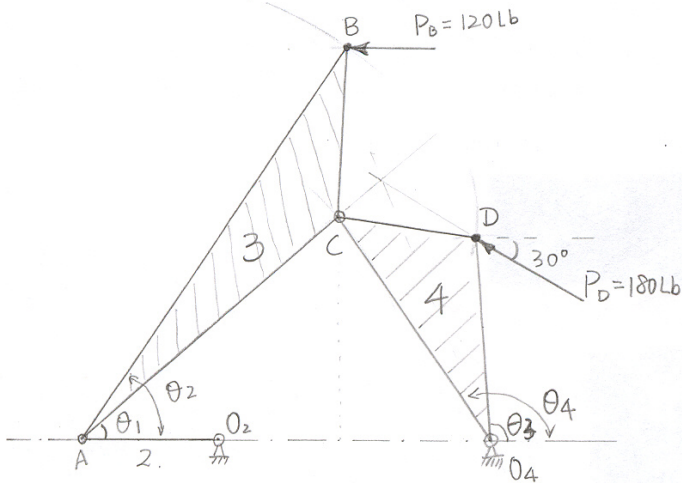
$$\vec{F}_{45} = -\vec{F}_{54} = -440.7 \hat{i} + 164.8 \hat{j} \text{ (N)}$$

$$\rightarrow \text{Link 5: } \vec{F}_{65} = -\vec{F}_{45} = 440.7 \hat{i} - 164.8 \hat{j} \quad \vec{F}_{56} = -\vec{F}_{65}$$

$$\rightarrow \text{Link 6: (No friction) } \left. \begin{array}{l} \vec{P} + \vec{F}_{56}^x = \vec{0} \\ \vec{F}_{16} + \vec{F}_{56}^y = \vec{0} \end{array} \right\} \rightarrow \begin{array}{l} \vec{P} = 440.7 \hat{i} \\ \vec{F}_6 = -164.8 \hat{j} \end{array}$$

Problem 1:

(i) Method of superposition: (Linear System).



Given:

$$R_{A0_2} = R_{C0_4} = 8 \text{ in}, \quad R_{A0_2} = 4 \text{ in}.$$

$$R_{CA} = 10 \text{ in}, \quad R_{BA} = 14 \text{ in},$$

$$R_{D0_4} = 6 \text{ in}, \quad R_{DC} = 4 \text{ in},$$

$$R_{BC} = 5 \text{ in},$$

$$P_B = 120 \text{ lb}, \quad P_D = 180 \text{ lb}, \quad \angle 120^\circ.$$

Kinematic Analysis: $\theta_1 = 41.41^\circ$, $\theta_2 = 55.98^\circ$, $\theta_3 = 95.27^\circ$, $\theta_4 = 124.23^\circ$.

Therefore, $\vec{R}_{A0_2} = -4\vec{i}$, $\vec{R}_{CA} = 7.5\vec{i} + 6.61\vec{j}$, $\vec{R}_{BA} = 7.83\vec{i} + 11.6\vec{j}$

$$\vec{R}_{C0_4} = -4.5\vec{i} + 6.61\vec{j}, \quad \vec{R}_{D0_4} = -0.55\vec{i} + 5.98\vec{j}.$$

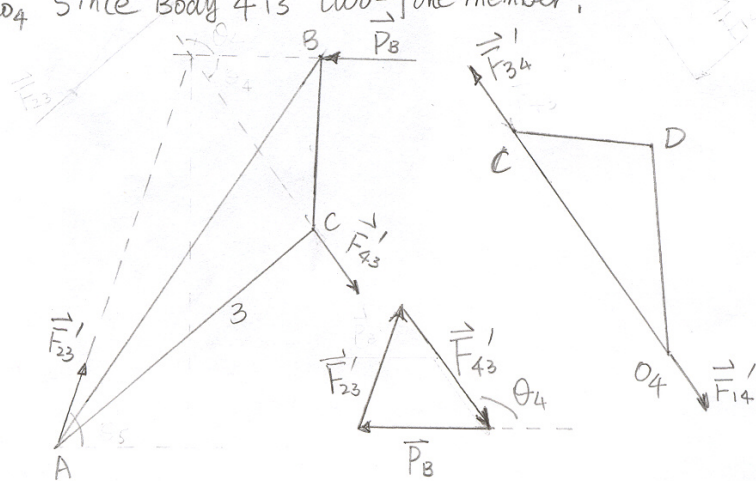
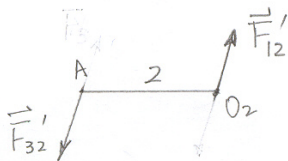
Force Analysis:

→ Starting with body 3 with $P_B = 120 \text{ lb} \angle 180^\circ$ (only). Note: The other Force \vec{F}_D is neglected in this part.

As shown below, we have the forces: $\vec{P}_B + \vec{F}'_{23} + \vec{F}'_{43} = 0$.

\vec{F}'_{23} , \vec{F}'_{43} is along with R_{C0_4} since Body 4 is two-force member.

→ For P_B .



For P_B , we have $\vec{P}_B + \vec{F}_{23}' + \vec{F}_{43}' = 0$,

Also consider the moment balance with respect to point A:

$$\sum \vec{M}_A' = \vec{R}_{BA} \times \vec{P}_B + \vec{R}_{CA} \times \vec{F}_{43}' = 0$$

Here

$$\vec{R}_{BA} \times \vec{P}_B = (7.83\vec{i} + 11.6\vec{j}) \times (-120\vec{i}) = 1392 \vec{k} \text{ lb}\cdot\text{in. ccw}$$

$$\begin{aligned} \vec{R}_{CA} \times \vec{F}_{43}' &= (7.5\vec{i} + 6.61\vec{j}) \times (F_{43} \cos \theta_4 \vec{i} + F_{43} \sin \theta_4 \vec{j}) \\ &= (7.5\vec{i} + 6.61\vec{j}) \times (-0.5625 F_{43} \vec{i} + 0.827 F_{43} \vec{j}) \\ &= 9.92 F_{43} \vec{k} = -1392 \vec{k} \text{ lb}\cdot\text{in} \end{aligned}$$

$$\therefore F_{43}' = -140.31 \text{ lb.} \quad \vec{F}_{43}' = 78.9\vec{i} - 116.04\vec{j} \text{ lb}$$

$$\vec{F}_{34}' = -78.9\vec{i} + 116.04\vec{j} \text{ lb} \quad \vec{F}_{14}' = -\vec{F}_{34}' = 78.9\vec{i} - 116.04\vec{j} \text{ lb}$$

By using $\vec{P}_B + \vec{F}_{23}' + \vec{F}_{43}' = 0$,

$$\begin{cases} -120 + F_{23}'_x + 78.9 = 0 \\ 0 + F_{23}'_y + (-116.04) = 0 \end{cases} \quad \therefore \vec{F}_{23}' = 41.1\vec{i} + 116.04\vec{j} \text{ (lb)}$$

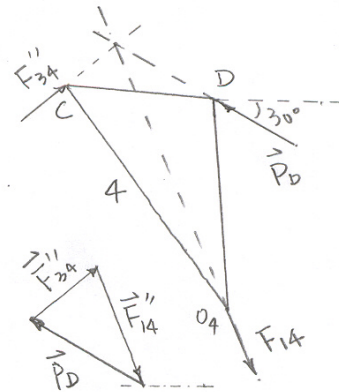
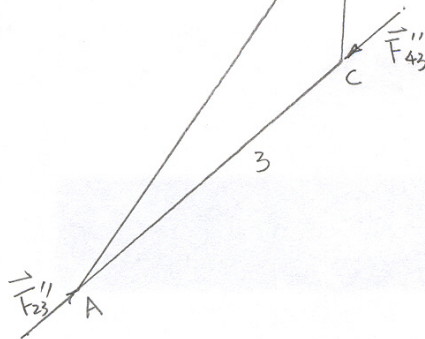
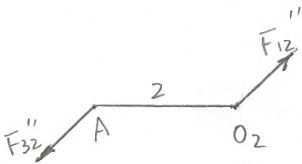
$$\text{Therefore, } \vec{F}_{32}' = -\vec{F}_{23}' = -41.1\vec{i} - 116.04\vec{j} \text{ lb}$$

$$\vec{M}_{12}' = -\vec{R}_{A0_2} \times \vec{F}_{32}' = -(-4\vec{i}) \times (-41.1\vec{i} - 116.04\vec{j}) = -464.16 \vec{k} \text{ lb}\cdot\text{in}$$

$$\text{Also, } \vec{F}_{72}' = 41.1\vec{i} + 116.04\vec{j} \text{ lb}$$

→ For P_D : [The other force \vec{F}_B is neglected here]

Note, \vec{F}_{34}'' along \vec{R}_{AC} since Body 3 is two-force member.



Analysis Solution:

For P_D , we have $\vec{P}_D + \vec{F}_{34}'' + \vec{F}_{14}' = 0$,

Also considering the moment balance about Point O_4 .

$$\sum \vec{M}_{O_4}'' = \vec{R}_{D O_4} \times \vec{P}_D + \vec{R}_{C O_4} \times \vec{F}_{34}'' = 0$$

Thus,

$$\vec{R}_{D O_4} \times \vec{P}_D = (-0.55\vec{i} + 5.98\vec{j}) \times (-180 \cos 30^\circ \vec{i} + 180 \sin 30^\circ \vec{j}) = 882.7 \vec{k} \text{ lb.in. (ccw)}$$

$$\vec{R}_{C O_4} \times \vec{F}_{34}'' = (-4.5\vec{i} + 6.6\vec{j}) \times (F_{34}'' \cos \theta_1 \vec{i} + F_{34}'' \sin \theta_1 \vec{j}) = -7.93 F_{34}'' \vec{k} = -882.7 \vec{k}$$

$$\therefore F_{34}'' = 111.25 \text{ lb.} \quad \vec{F}_{34}'' = 83.44 \vec{i} + 73.59 \vec{j} \text{ lb}$$

$$\therefore \vec{F}_{14}'' = -\vec{P}_D - \vec{F}_{34}'' = 72.44 \vec{i} - 163.59 \vec{j} \text{ lb}$$

$$\text{From } \left. \begin{array}{l} \text{Body 3} \\ \text{Body 2} \end{array} \right\}, \quad \vec{F}_{43}'' = -\vec{F}_{34}'' = -83.44 \vec{i} - 73.59 \vec{j} \text{ lb}$$

$$\vec{F}_{23}'' = -\vec{F}_{43}'' \Rightarrow \vec{F}_{32}'' = -\vec{F}_{23}'' = 83.44 \vec{i} + 73.59 \vec{j} \text{ lb}$$

$$\therefore \vec{M}_{12}'' = -\vec{R}_{A O_2} \times \vec{F}_{32}'' = (-4\vec{j}) \times (83.44 \vec{i} + 73.59 \vec{j}) = -294.36 \vec{k} \text{ lb.in}$$

$$\vec{M}_{12}'' = \vec{M}_{23}'' = 83.44 \vec{i} + 73.59 \vec{j} \text{ lb}$$

Final Answer: $F_{12} = F_{23} = 83.44 \text{ lb}$

Consequently, the results of Superposition of both forces, \vec{F}_B and \vec{F}_D , can be obtained:

- The moment on Crank 2:

$$\begin{aligned}\vec{M}_{12} &= \vec{M}'_{12} + \vec{M}''_{12} = -464.16\vec{k} - 294.36\vec{k} \\ &= -758.52\vec{k} \text{ lb}\cdot\text{in}\end{aligned}$$

- The constraint forces:

$$\begin{aligned}\vec{F}_{12} &= \vec{F}'_{12} + \vec{F}''_{12} = (41.1\vec{i} + 116.04\vec{j}) + (83.44\vec{i} + 73.59\vec{j}) \\ &= 124.54\vec{i} + 189.63\vec{j} \text{ lb}\end{aligned}$$

$$\vec{F}_{32} = \vec{F}'_{32} + \vec{F}''_{32} = -124.54\vec{i} - 189.63\vec{j} \text{ lb}$$

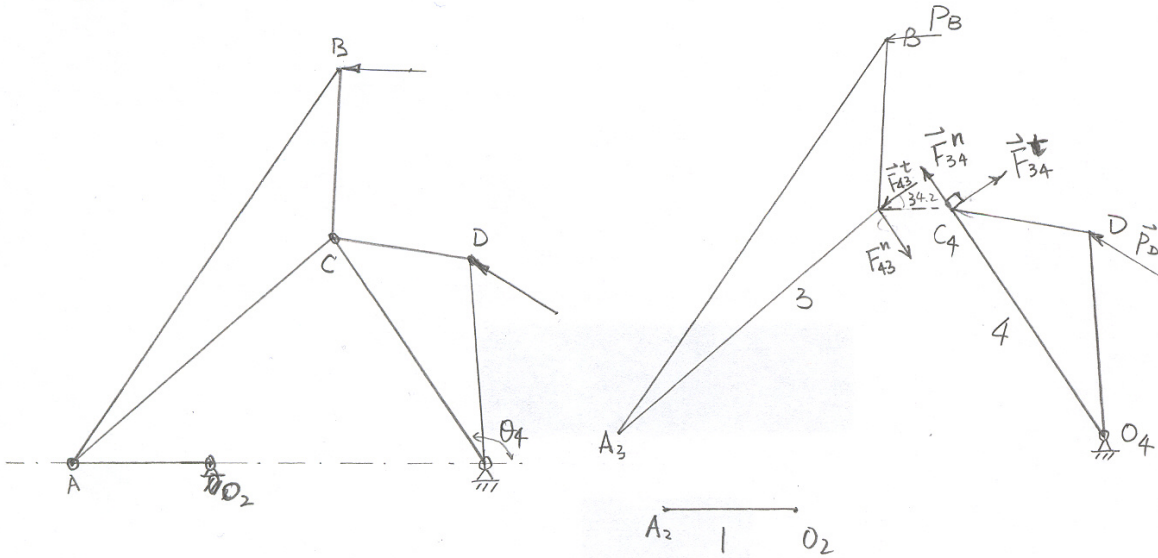
Note, $\vec{F}_{23} = -\vec{F}_{32}$.

$$\begin{aligned}\vec{F}_{43} &= \vec{F}'_{43} + \vec{F}''_{43} = 78.9\vec{i} - 116.04\vec{j} - 83.4\vec{i} - 73.59\vec{j} \\ &= -4.5\vec{i} - 189.63\vec{j} \text{ lb}\end{aligned}$$

$$\vec{F}_{34} = -\vec{F}_{43} = 4.5\vec{i} + 189.63\vec{j} \text{ N.}$$

$$\begin{aligned}\vec{F}_{14} &= \vec{F}'_{14} + \vec{F}''_{14} = 78.9\vec{i} - 116.04\vec{j} + 72.44\vec{i} - 163.59\vec{j} \\ &= 151.4\vec{i} - 296.9\vec{j} \text{ lb}\end{aligned}$$

(ii) Method II:



Decompose the system into parts, and first consider Body 4,

$$\begin{aligned}\sum M_{O_4} &= \vec{R}_{D O_4} \times \vec{P}_D + \vec{R}_{C_4 O_4} \times \vec{F}_{34}^t \\ &= (-0.55\vec{i} + 5.97\vec{j}) \times (-156\vec{i} + 90\vec{j}) + \vec{R}_{C_4 O_4} \times \vec{F}_{34}^t\end{aligned}$$

$$\begin{aligned}\therefore F_{34}^t &= 110.3 \text{ lb} < 34.23. \quad \text{or } \vec{F}_{34}^t = 91\vec{i} + 62\vec{j} \text{ lb.} \\ F_{43}^t &= -91\vec{i} - 62\vec{j} \text{ lb.}\end{aligned}$$

Now consider body 3, the moment with respect to A:

$$\sum M_A = 0 = \vec{R}_{BA} \times \vec{P}_B + \vec{R}_{CA} \times \vec{F}_{43}^t + \vec{R}_{CA} \times \vec{F}_{43}^n$$

Hence, $\vec{R}_{BA} \times \vec{P}_B = 1392\vec{k} \text{ lb}\cdot\text{in}.$

$$\vec{R}_{CA} \times \vec{F}_{43}^t = (7.5\vec{i} + 6.6\vec{j}) \times (-91\vec{i} - 62\vec{j}) = -136.9\vec{k} \text{ lb}\cdot\text{in}.$$

$$\therefore F_{43}^n (7.5\vec{i} + 6.6\vec{j}) \times [\cos(-55.8)\vec{i} + \sin(-55.8)\vec{j}] = 9.91 F_{43}^n = 1392 + 136.9$$

$$\therefore \vec{F}_{43}^n = 154.2 < -55.8^\circ. \quad \text{or } \vec{F}_{43}^n = 86.7\vec{i} - 127.6\vec{j} \text{ lb.}$$

$$\therefore \vec{F}_{43} = \vec{F}_{43}^n + \vec{F}_{43}^t = -4.3\vec{i} - 189.6\vec{j} \text{ lb}$$

Thus $\vec{F}_{34} = -\vec{F}_{43} = 4.3\vec{i} + 189.6\vec{j} \text{ lb.}$

Now, from the force balance:

Body 4:

$$\vec{F}_{14} = -\vec{P}_D - \vec{F}_{34} = +152\vec{i} - 279\vec{j} \text{ lb}$$

Body 3:

$$\begin{aligned}\vec{F}_{23} &= -\vec{P}_B - \vec{F}_{43} = 120\vec{i} + 4.3\vec{i} + 189.6\vec{j} \\ &= 124.3\vec{i} + 189.6\vec{j} \cdot \text{lb}\end{aligned}$$

Body 2:

$$\therefore \vec{F}_{32} = -124.3\vec{i} - 189.6\vec{j} \text{ lb}$$

$$\begin{aligned}\vec{M}_{12} &= -\vec{R}_{A02} \times \vec{F}_{32} = -(4.0\vec{i}) \times (-124.3\vec{i} - 189.6\vec{j}) \\ &= -758.4 \vec{k} \text{ lb}\cdot\text{in. cw.}\end{aligned}$$