

1. Introduction

- **Motivation:** When two or more robots work together, they may need to meet or *rendezvous* first.
- **Goal:** We consider the case where multiple robots have been deployed in an unknown bounded environment at unknown locations and are unable to communicate unless they are co-located. In such a scenario, the robots must find one another to speed-up the exploration task.

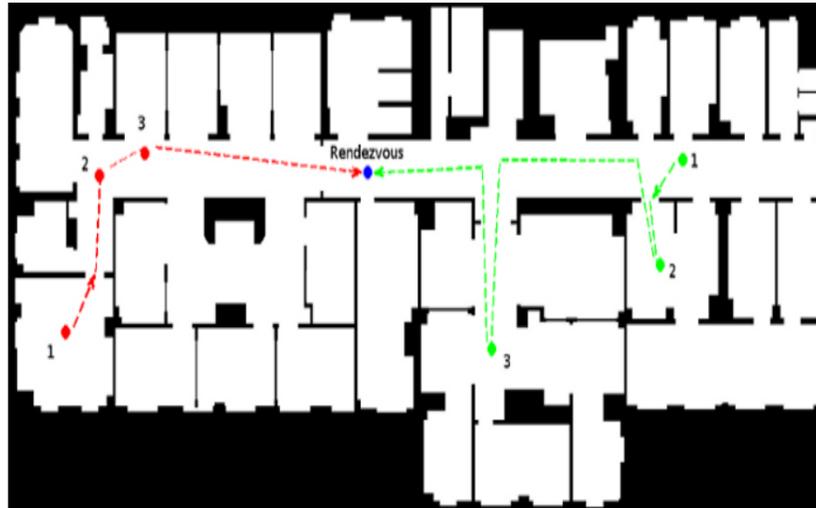


Fig.1: A rendezvous simulation of two robots

2. Proposed Approach

- An energy efficient combination of exploration and rendezvous is proposed and its overview is presented in Fig. 2.
- The robots initially discover potential rendezvous locations while exploring the unknown environment.
- These locations are ordered using different *ranking criteria* and visited during the rendezvous phase using the following strategies:
 - **asymmetric:** (a.k.a) "wait for mommy" [1], where one robot waits while the others search
 - **symmetric:** All robots search and have symmetric behaviors
 - **exponential:** The robots visit ranked locations based on exponential probability.

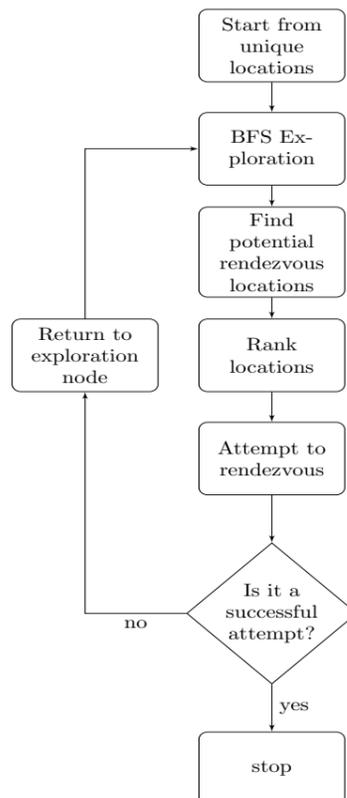


Fig.2: Combining exploration and rendezvous [3]

3. Ranking Criteria

- Our ranking criteria are based on a *cost-reward* model which considers the distinctiveness $D(p_k)$ of a potential rendezvous location p_k as measured by robot k , to find other robots, along with its distance $d(c_k, p_k)$ from its current location c_k .
- This model helps to reduce the total travel time in case of unsuccessful rendezvous attempts and also increases the area explored.
- The following are two variants of the model:
 - **linear distance-based ranking:**

$$L(p_k) = \frac{D(p_k)}{d(c_k, p_k)} \quad (1)$$

- **sigmoid distance-based ranking:**

$$S(p_k) = \frac{D(p_k)}{\text{sigmoid}(d(c_k, p_k))} \quad (2)$$

4. Simulation Results

- The performance of the ranking criteria and rendezvous strategies for three robots in an abstract environment were compared with respect to the time taken to rendezvous.
- These results are shown in Fig. 3 which illustrate that the asymmetric rendezvous strategy and sigmoid-distance based ranking criterion performed the best.

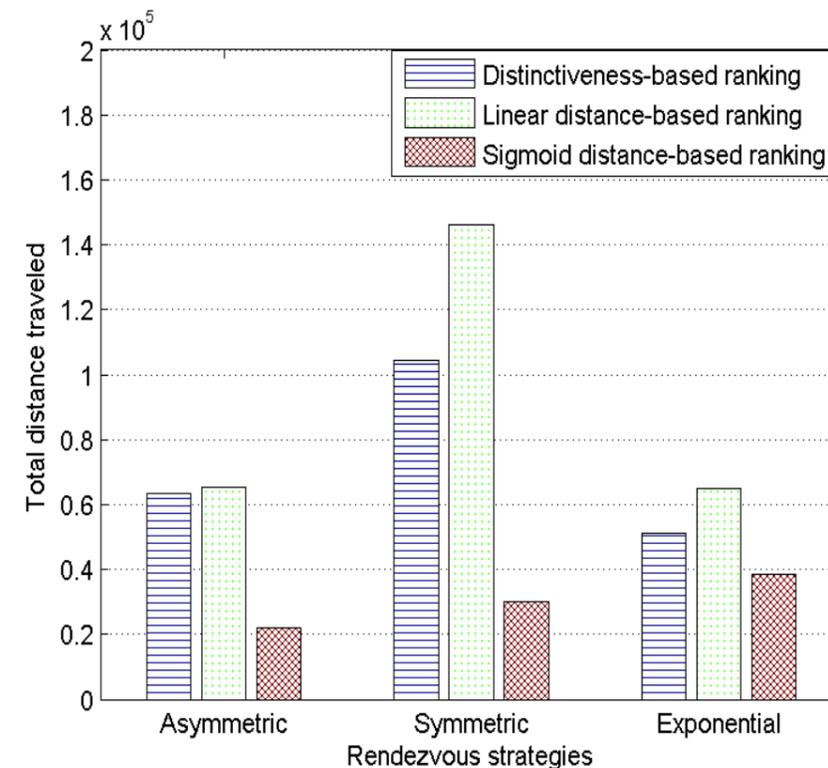


Fig.3: Total distance traveled for different rendezvous strategies and ranking criteria

5. Hybrid Ranking

- The cost-reward model (sigmoid-based ranking) is most effective when there is less overlap and the distinctiveness measure is useful with more overlap.
- Thus, we propose a combination of the two ranking criteria based on the area explored using the following hybrid ranking $D'(p_k)$:

$$D'(p_k) = (1 - \alpha)D(p_k) + \alpha \frac{D(p_k)}{d(c_k, p_k)} \quad (3)$$

- α in the above equation is a weighting function which is inversely proportional to the area explored. These results are presented in Fig. 4.

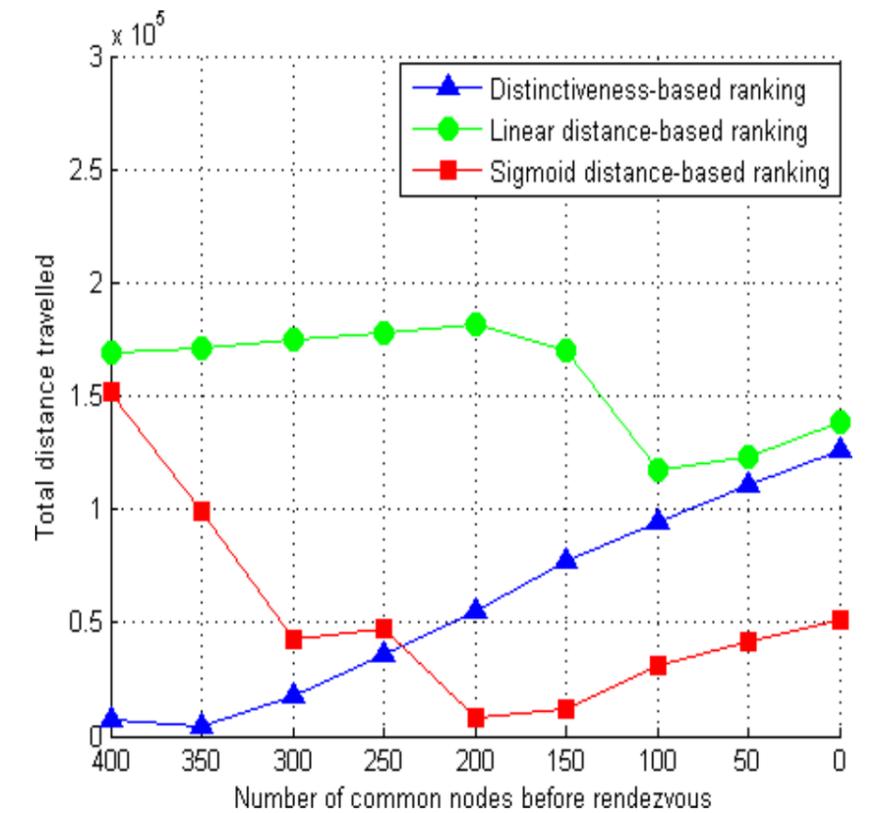


Fig.4: Hybrid ranking criterion

6. Conclusion

- Efficient combination of multi-robot exploration and rendezvous tasks.
- Cost-reward model was shown to be a better ranking criterion than pure distinctiveness-based ranking.
- Hybrid-ranking criterion was proposed to capture the best aspects of distinctiveness and cost-reward model based ranking.

7. References

- [1]. S. Alpern and S. Gal. *The theory of search games and rendezvous*. Springer, 2003.
- [2]. N.Roy and G.Dudek. *Collaborative exploration and rendezvous: algorithms, performance bounds and observations*. Autonomous Robots 2001.
- [3]. M.Meghjani and G. Dudek. *Combining Multi-robot exploration and rendezvous*. Canadian Conference on Computer and Robot Vision 2011.