lecture 5

Sequential circuits 1

- RS latch
- D latch
- flipflops (D)
- registers

January 25, 2016
- truth tables and circuit diagrams
- 0 and 1 signals are (voltage) values on wires
- circuits take time to "compute" e.g. carries in addition
this week....

• combinational circuits + memory

• synchronized by a clock C
Memory (two kinds)

- write it down

- repeat it to yourself (feedback)

Sequential circuits use the latter.
Latch

definition (wikipedia); ".. a type of ... fastener that is used to join two objects or surfaces together while allowing for the regular ... separation of the surfaces"

Latches are often (but not always) used to block paths, e.g. close doors.
RS latch ('reset' 0, 'set' 1)

\[
\begin{array}{c|c|c|c|c}
A & B & A+B & \overline{A+B} \\
\hline
0 & 0 & 0 & 0 \\
0 & 1 & 1 & 0 \\
1 & 0 & 1 & 0 \\
1 & 1 & 1 & 0 \\
\end{array}
\]
\[ R = S = 1 \]

inputs will not be allowed.

\[
\begin{array}{c|c|c|c}
A & B & A + B & \overline{A + B} \\
\hline
0 & 0 & 0 & 1 \\
0 & 1 & 1 & 0 \\
1 & 0 & 1 & 0 \\
1 & 1 & 0 & 0 \\
\end{array}
\]
<table>
<thead>
<tr>
<th>A</th>
<th>B</th>
<th>A + B</th>
<th>\overline{A + B}</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0</td>
<td>0</td>
<td>1</td>
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<td>0</td>
</tr>
</tbody>
</table>
\[
\begin{array}{ccc}
A & B & A+B \\
0 & 0 & 0 \\
0 & 1 & 1 \\
1 & 0 & 1 \\
1 & 1 & 0 \\
\end{array}
\]
\( Q, \overline{Q} \) values do not change (memory)

<table>
<thead>
<tr>
<th>A</th>
<th>B</th>
<th>A+B</th>
<th>\overline{A+B}</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0</td>
<td>0</td>
<td>1</td>
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</table>
The diagram shows a circuit with inputs R and S, and outputs Q and Q'. The truth table below summarizes the behavior of the circuit:

<table>
<thead>
<tr>
<th>R</th>
<th>S</th>
<th>Q</th>
<th>Q'</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0</td>
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</tbody>
</table>

The notation 'hold previous values' implies that when both R and S are 0, the circuit holds the previous values of Q and Q'.
- electronic implementation uses "crystal oscillator"
  https://en.wikipedia.org/wiki/Clock_signal

- typical clock speed is in gigahertz \((10^9 \text{ cycles/sec})\)
Clocked RS latch
D latch ("D" is for data)

What does this circuit do?

When $C = 1$, $D = 1$ $\Rightarrow$ $Q = 1$, $\bar{Q} = 0$

When $C = 0$, $D = 0$ $\Rightarrow$ $Q = 0$, $\bar{Q} = 1$

When $C = 0$, hold values of $Q$, $\bar{Q}$
D latch

$C = 0$ holds values in D latches.  (Read only)

$C = 1$ allows values in D latches to go through.  
(Read and write).
Example:

Suppose we used D latches to store 8 bit numbers A and B. Suppose we added A and B using the circuit below and wrote the new value back into B. Would this work? No, because when C = 1 there would be no control over timing and we could loop through multiple times within a single clock pulse (while C = 1).
D flip flop

\[ C = 1 \]  
Write D value into first D latch.  
Q doesn't change.

\[ C = 0 \]  
Stop writing D into first D latch.  
The D value from first D latch is written into second, so Q gets a possibly new value.
D flip flop  ("falling edge triggered")

example
D flip flop ("rising edge triggered")

By putting the inverter on the first D latch, we would make Q change its value on the rising edge of the clock. There is no advantage to this, so for simplicity we will always work with falling edge triggered. I will use this next lecture.
Clock cycle must be long enough to allow all gates to stabilize.

Clock synchronizes all flipflops, allowing us to treat time as a sequence of discrete read/write steps (hence 'sequential circuit')

From now on,

- we ignore all variations within a clock cycle
  e.g. carries in the adder.

- we work only with D flipflops (no more latches)
Register

(set of flipflops that are read/written together)
Example:

suppose at \( t = 0 \).

\((Q4, Q3, Q2, Q1, Q0)\)
is \((0, 1, 0, 0, 1)\)

Q4 remains at 0 for the five clock pulses shown.

What happens at each falling edge of clock?
Shift Right Register

We can make Q4 have other values e.g. D (variable), 1, 0, Q0.

We can then select which of these gets put into the MSB.
Shift Left Register

Alternatively, physically order the flipflops in the opposite order
Select from:
- shift left
- shift right
- write data
- clear
Announcements

- Quiz 1 and yellow sticky notes

- Assignment 1
  - plan is to post next monday (you'll have ~10 days)
  - download logisim from public web page link, and familiarize yourself with tutorial

- Quizzes 2-6 will take place in ARTS 145 (lastname to be determined - see announcements)