

From Search to Games



FEB
10

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THIS DAY IN **HISTORY**

Sports

1996

Deep Blue beats Kasparov at chess

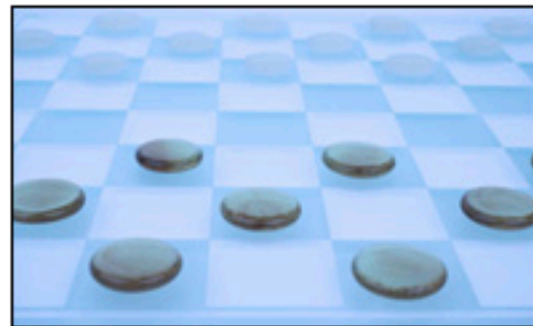
Computers Solve Checkers—It's a Draw

King me! Top computer scientist proves perfect play leads to draw, recounts battle for world championship, gets kinged

By JR Minkel | July 19, 2007

Jonathan Schaeffer's quest for the perfect game of checkers has ended. The 50-year-old computer scientist from the University of Alberta in Edmonton left human players in the dust more than a decade ago after a trial by fire against the greatest checkers champion in history.

And now, after putting dozens of computers to work night and day for 18 years—*jump, jump, jump*—he says he has solved the game—*king me!* "The starting position, assuming no side makes a mistake, is a draw," he says.



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January 2015

Heads-up limit Texas hold 'em poker solved by University of Alberta scientists

Poker algorithm another step toward artificial intelligence

By Aleksandra Sagan, [CBC News](#) | Posted: Jan 08, 2015 3:39 PM ET | Last Updated: Jan 08, 2015 3:39 PM ET



Scientists at the University of Alberta have essentially solved heads-up limit hold 'em poker with an algorithm they hope will lead to advances in artificial intelligence. (Shutterstock)

Readings for this class

- Chapter 5-5.4

Learning Objectives

- how to describe a game in AI terms
- basic concepts of game-theory
- how the minimax algorithm finds an optimal move
- benefits of alpha-beta pruning
- simple strategies for position evaluation functions

From problem formulation to game defn

- **states**: description of “world of interest”
- **initial state**
- **successor function**: generates set of legal next states from available actions
- **goal test** → **terminal test**: when is game over?
- **path cost** → **utility function**: value of terminal states

Why search won't work

- search for sequence of moves that leads to terminal state with positive utility (winning state)
- opponent might not be so cooperative!

Optimal Decisions in 2-player games

- solution: find strategy that leads to winning state regardless of what opponent does

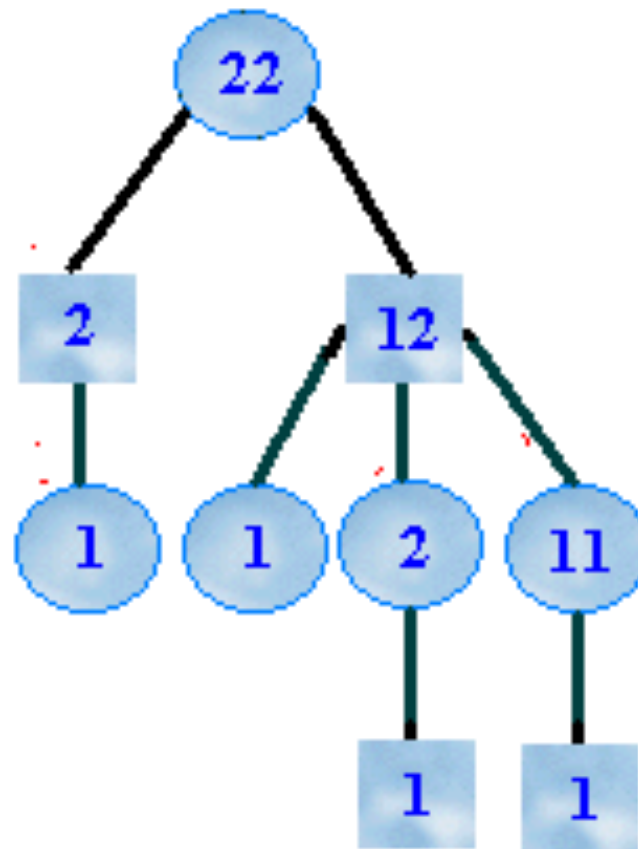
Minimax strategy for 2-player games

- generate whole game tree down to terminal nodes
- find value of each terminal state using **utility function**
- repeat
 - determine utility of parent nodes from children
 - **MIN** chooses move that minimizes utility
 - **MAX** chooses move that maximizes utility
- until we reach root
- choose move that leads to “best” value

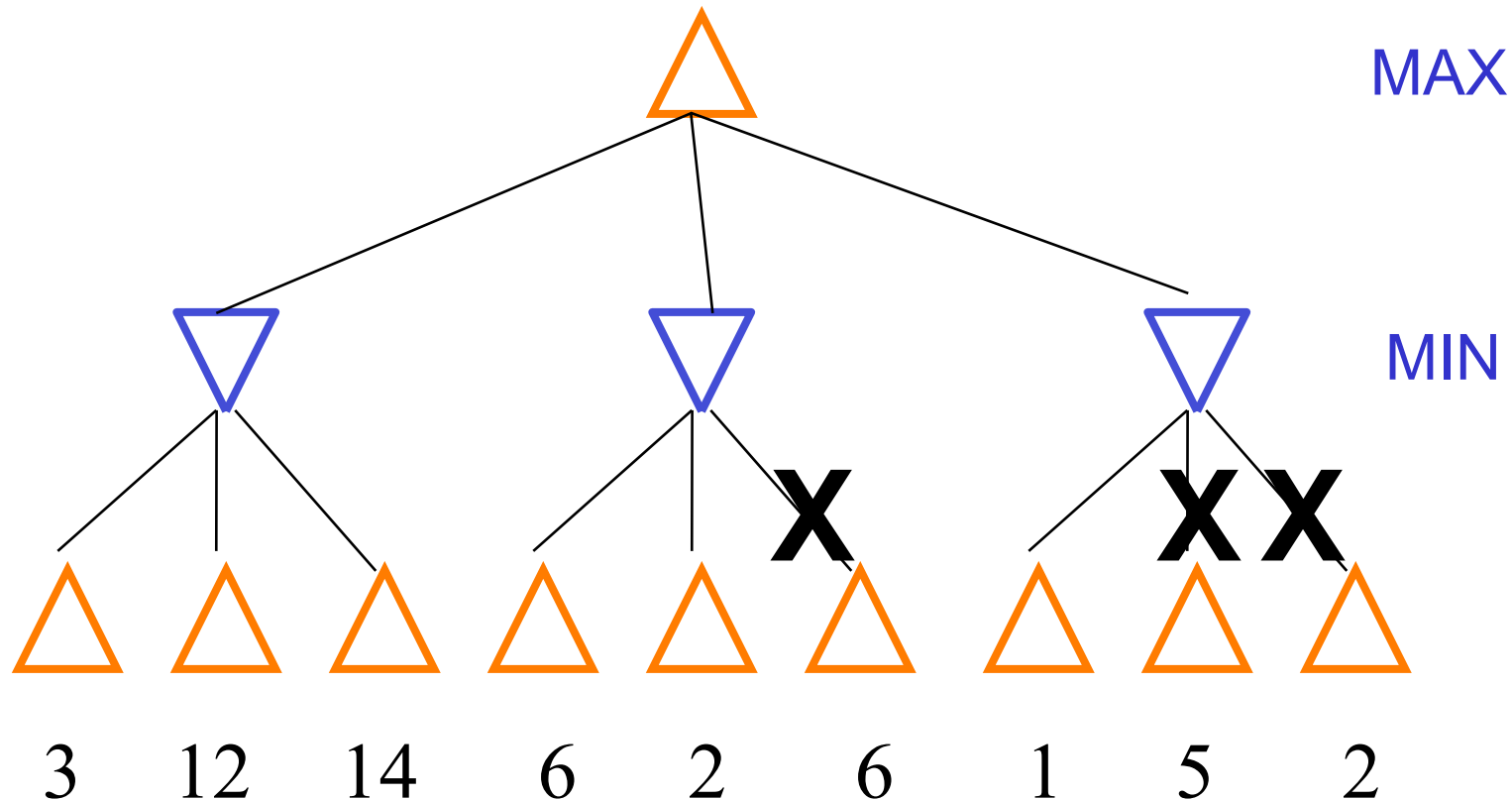
MiniMax algorithm

```
minmax(u) { // u is node to evaluate
  if u is a leaf return score of u;
  else if u is a min node
    for all children of u: v1, .. vn
      return min{ minmax(v1),..., minmax(vn)}
  else // u is a max node
    for all children of u: v1, .. vn
      return max{ minmax(v1),...,minmax(vn)}
}
```

NIM - player to take last stick loses



Improved search with alpha-beta pruning



stops evaluating a move when at least one possibility has been found that proves the move to be worse than a previously examined move

Alpha-Beta pseudocode

// from https://en.wikipedia.org/wiki/Alpha%E2%80%93beta_pruning

// initial call is: **alphabeta**(origin, depth, $-\infty$, $+\infty$, TRUE)

```
function alphabeta(node, depth,  $\alpha$ ,  $\beta$ , maximizingPlayer)
  if depth = 0 or node is a terminal node
    return the heuristic value of node
  if maximizingPlayer
     $v := -\infty$ 
    for each child of node
       $v := \max(v, \text{alphabeta}(\text{child}, \text{depth} - 1, \alpha, \beta, \text{FALSE}))$ 
       $\alpha := \max(\alpha, v)$ 
      if  $\beta \leq \alpha$  break (*  $\beta$  cut-off *)
    return v
  else
     $v := \infty$ 
    for each child of node
       $v := \min(v, \text{alphabeta}(\text{child}, \text{depth} - 1, \alpha, \beta, \text{TRUE}))$ 
       $\beta := \min(\beta, v)$ 
      if  $\beta \leq \alpha$  break (*  $\alpha$  cut-off *)
    return v
```

Problem

- usually impossible to explore entire state space (e.g., chess search tree has approx. 35^{100} nodes)
- infeasible to make optimal decision
- solution: use heuristic position evaluators – an estimate of utility of states based on insight

Position Evaluators

- game specific: have to be creative
- what are the determining factors in the goodness of a game state (utility)?
 - e.g., chess:
 - Sum of point value of pieces
 - Control of centre of board
 - Pawn structure
 - Defence of king
 - Mobility of pieces

Homework

- **Read before next class:**
 - Ch. 2
 - Brooks, A Robust Layered Control System for a Mobile Robot