

# *Compact and Efficient Generation of Radiance Transfer for Dynamically Articulated Characters*

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# Goal, Challenges & assumptions

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- Self-shadowing of a *dynamically* articulating character mesh
  - Under varying external illumination
  - High-performance ( $> 100$  Hz)
- Per-vertex visibility is prohibitively expensive to calculate every frame
- Diffuse-only characters
- Direct-illumination
- Low-frequency distant lighting and shading

# Previous Work

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- Kirk and Arikian, Kontkanen and Aila
  - AO as a linear function of joint angles
- Ren et al. abstract animating geometry with spheres and use SH log space accumulation
- Zhou et al. precompute shadow fields for rigid motion

# Main Idea

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- Given a training animation,  $\mathbf{f}$  frames long, of a mesh with  $\mathbf{v}$  vertices:
  1. Precompute the per-vertex/per-frame cosine-weighted visibility functions (expensive)
  2. SH project these spherical functions, yielding  $\mathbf{c}$  coefficients (per-vertex, per-frame =  $\mathbf{fvc}$  floats in a training set)
- Can we fit a linear model of the joint angles to this dataset?
- Is more aggressive compression possible/useful?

# Is a Linear Model Sufficient?

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- We show empirically that a linear model of the joint angles sufficiently fits the SH projected cosine-weighted visibility data
- Statistically speaking:
  - We show training and test error
  - Residual distribution

# Why the Linear Model is Good

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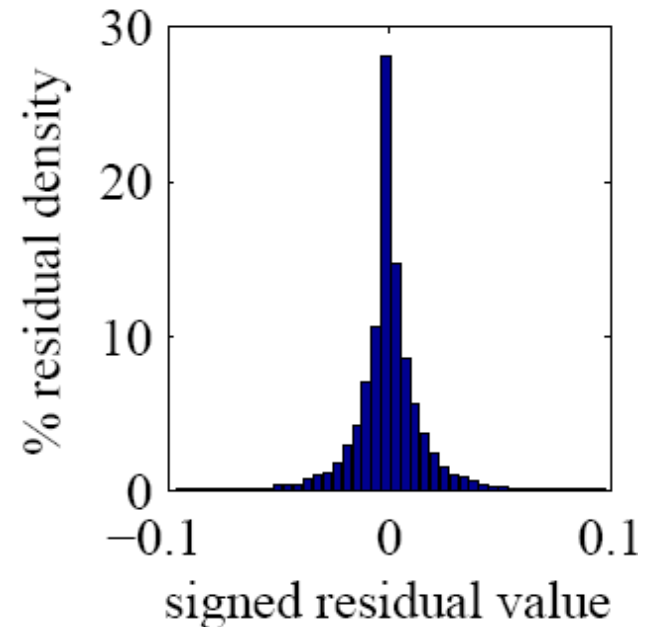
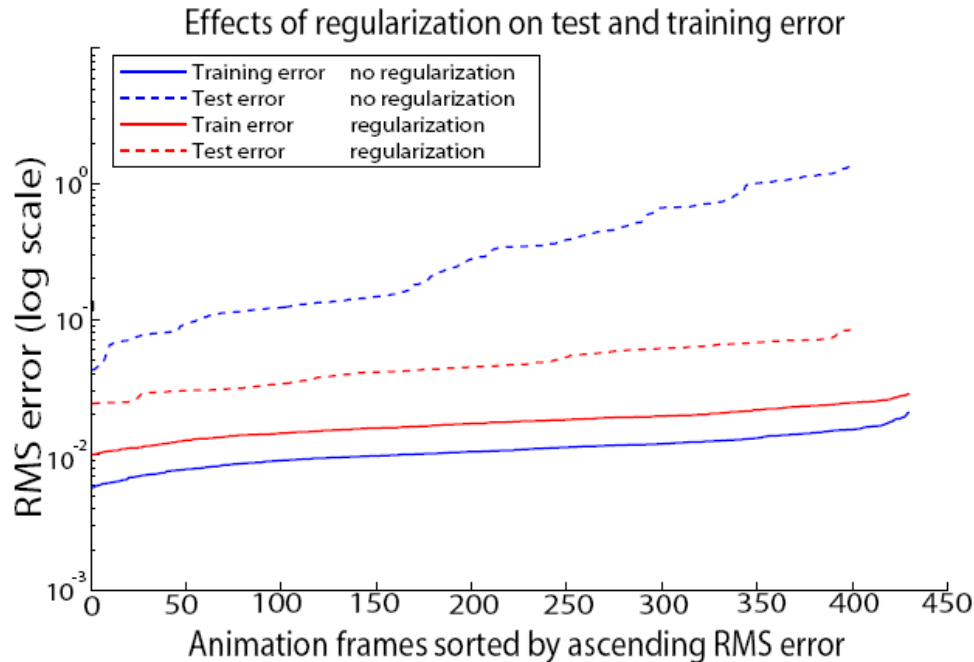
- Sufficient reconstruction of the dataset
- Optimally solvable in closed form
- Smooth by construction
  - Consistent, plausible results
- Compact representation (as small as 1MB)
- Very fast to evaluate (100 Hz, including shading)

# Regularization

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- Our technique can be used solely as a compression method for animated shadowing data
- But, in general, we want to train on a small (representative) dataset and *generalize* well to unseen poses
- We apply regularization to get sensible (actually, very sensible) reconstruction error for dynamically articulated animations

# Empirical Proof of Linearity



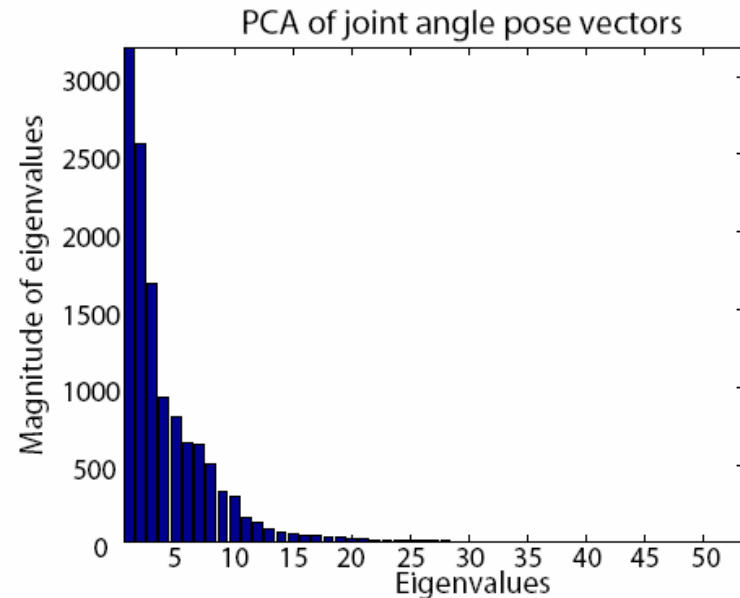
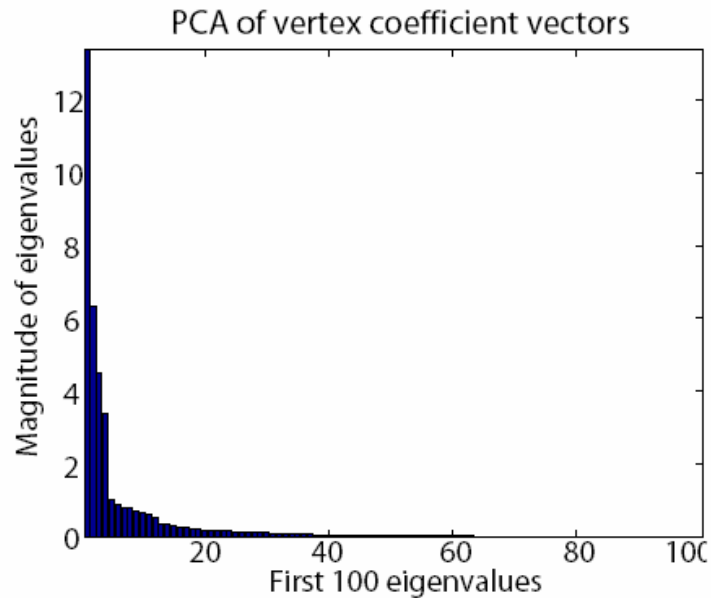


# Dimensionality Reduction

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- Given an articulated character with  $\mathbf{a}$  joint angles:
  - for each of the  $\mathbf{c}$  coefficients, we have a linear mapping,  $\mathbf{X}$  of size  $\mathbf{a} \times \mathbf{v}$
- Observations:
  1. PCA over joint angles shows high variance in only the first few eigenvectors
  2. PCA over each SH coefficient at vertices also yields a similar, yet less pronounced, drop-off of variance

# Visual Artifacts due to PCA



22 eigenvalues (90% variance)



500 eigenvalues (99% variance)



1000 eigenvalues (99.9% variance)

# Run-time Reconstruction

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No Dimensionality Reduction:

1. Query joint angles
2. Perform  $\mathbf{c}$  vector/matrix multiplications with linear models  
→ This yields the  $\mathbf{c}$  SH cosine-weighted visibility coefficients
3. Dot the currently generated per-vertex SH coefficients with the external lighting coefficients → Final shade

# Run-time Reconstruction cont...

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With Dimensionality Reduction:

1. Query joint angles
2. Project joint angle vector to lower-dimensional joint angle vector
3. Perform  $\mathbf{c}$  vector/matrix multiplications with reduced linear models
4. Reproject low-dimensional coefficients to original number of vertices
5. Dot the currently generated per-vertex SH coefficients with the external lighting coefficients  $\rightarrow$  Final shade

# Storage Requirements

Master Pai (11.5k vertices & 54 joint angles) Trained on a 430 frame animation.			
	Memory: Absolute	Memory: % of total data	Memory: % of 1 mesh's data
Linear Model (No PCA reduction)	87.5MB	12.56%	5400%
PCA (15,500)	23.6MB	3.39%	1457%
PCA (8,22)	<b>1.0MB</b>	<b>0.146%</b>	<b>62.9%</b>

Armadillo (24.9k vertices & 25 joint angles) Trained on a 250 frame animation.			
	Memory: Absolute	Memory: % of total data	Memory: % of 1 mesh's data
Linear Model (No PCA reduction)	85.4MB	10.0%	2500%
PCA (15,500)	48.6MB	5.68%	1421.13%
PCA (8,22)	<b>2.1MB</b>	<b>0.248%</b>	<b>61.93%</b>

# Conclusions

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- A linear function of joint angles captures low-frequency shadowing effects on:
  - Training animation sequences, and
  - Dynamically generated (test) animation
- Dimensionality reduction allows to further trade reconstruction accuracy with storage requirements

# Thank you! Questions?

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